

Engaging in the Mathematical Practices (Look-fors)

Mathematical Practices		Students:	Teachers:
Overarching Habits of Mind	1. Make sense of problems and persevere in solving them	<input type="checkbox"/> Explain the meaning of the problem and look for entry points to its solution. <input type="checkbox"/> Analyze and organize information (givens, constraints, relationships, goals). <input type="checkbox"/> Make conjectures and plan a solution pathway. <input type="checkbox"/> Consider analogous problems and try special cases. <input type="checkbox"/> Use different representations of the problem to understand and solve it. <input type="checkbox"/> Monitor and evaluate progress on the problem and change course as needed. <input type="checkbox"/> Check answers to problems and ask, "Does this make sense?" <input type="checkbox"/> Understand the approaches of others and identify connections between different approaches.	<input type="checkbox"/> Involve students in rich problem-based tasks that encourage them to persevere in order to reach a solution. <input type="checkbox"/> Provide opportunities for productive struggle and help students persevere by providing just-in-time scaffolds and checking in with them to help them clarify their thinking and process. <input type="checkbox"/> Provide opportunities for students to solve problems that have multiple approaches and solutions. <input type="checkbox"/> Encourage students to represent their thinking while problem solving. <input type="checkbox"/> Use tasks that lend themselves to multiple representations.
	6. Attend to precision	<input type="checkbox"/> Communicate precisely to others using clear definitions and math vocabulary. <input type="checkbox"/> State the meaning of symbols they use and use them appropriately. <input type="checkbox"/> Specify units of measure when working with quantities. <input type="checkbox"/> Calculate accurately and efficiently, expressing numerical answers with a degree of precision appropriate for the problem context. <input type="checkbox"/> Provide carefully formulated explanations. <input type="checkbox"/> Accurately label diagrams and axes to clarify the correspondence with quantities in the problem.	<input type="checkbox"/> Help students learn math definitions by bridging the gap between informal math language and formal terminology as students engage in mathematical explorations and experiences. <input type="checkbox"/> Consistently model precise communication with notation and vocabulary. <input type="checkbox"/> Encourage students to focus on the clarity of the definitions, notation, and vocabulary used to convey their reasoning. <input type="checkbox"/> Help students consider the accuracy and efficiency of computation and problem-based solutions.
Reasoning and Explaining	2. Reason abstractly and quantitatively	<input type="checkbox"/> Make sense of quantities and their relationships in problem situations. <input type="checkbox"/> Decontextualize: abstract a given situation and represent it symbolically. <input type="checkbox"/> Contextualize: relate the symbolic representation of a problem back to the situation it represents. <input type="checkbox"/> Create a coherent representation of the problem at hand. <input type="checkbox"/> Consider the units involved in a problem. <input type="checkbox"/> Know and flexibly use different properties of operations and objects.	<input type="checkbox"/> Help students understand the relationship between a problem scenario and its mathematical representation. <input type="checkbox"/> Encourage students to use properties of operations and objects when solving problems. <input type="checkbox"/> Ask how, why, and when questions to prompt students to reflect on their reasoning.
	3. Construct viable arguments and critique the reasoning of others	<input type="checkbox"/> Understand and use stated assumptions, definitions, and previously established results in constructing arguments. <input type="checkbox"/> Construct arguments and justify conclusions using objects, drawings, diagrams, and/or actions. <input type="checkbox"/> Make conjectures and build a logical progression of statements to explore the truth of their conjecture. <input type="checkbox"/> Listen to or read the arguments of others, decide whether they make sense, and ask useful questions to clarify or improve the argument. <input type="checkbox"/> Compare arguments and distinguish correct logic or reasoning from that which is flawed, and—if there is a flaw in an argument—explain what it is. <input type="checkbox"/> Analyze situations by breaking them into cases and use counterexamples to show a statement if false.	<input type="checkbox"/> Provide opportunities for students to explain their thinking aloud and encourage them to use objects, drawings, diagrams, and/or actions to support their explanations. <input type="checkbox"/> Provide opportunities for students to listen to and compare the solution strategies of others. <input type="checkbox"/> Provide opportunities for students to engage in explorations and/or investigations and make conjectures. <input type="checkbox"/> Provide opportunities for error analysis.

	Mathematical Practices	Students:	Teachers:
Modeling and Using Tools	4. Model with mathematics	<input type="checkbox"/> Apply the math they know to solve problems arising in everyday life, society, and the workplace. <input type="checkbox"/> Use assumptions and approximations to simplify a complicated situation. <input type="checkbox"/> Decide which tools and methods to use to solve the problem. <input type="checkbox"/> Identify important quantities in a situation and model their relationships using diagrams, two-way tables, graphs, flowcharts, and/or formulas. <input type="checkbox"/> Check to see if an answer makes sense within the context of the situation and improve the model if necessary.	<input type="checkbox"/> Use real-world scenarios that interest students and pose, or ask students to pose, questions that require the use of mathematics to solve. <input type="checkbox"/> Use tasks that require students to make decisions about how to approach a problem mathematically. <input type="checkbox"/> Help students understand the context of the problem. <input type="checkbox"/> Remind students that a mathematical model used to represent a problem's solution is 'a work in progress,' and may be revised as needed.
	5. Use appropriate tools strategically	<input type="checkbox"/> Consider available tools (e.g., pencil and paper, ruler, compass, protractor, calculator, concrete models, digital technologies,) when solving a problem and know when and how to use the tool. <input type="checkbox"/> Use technological tools to explore and deepen understanding of concepts.	<input type="checkbox"/> Provide students access to a variety of physical and digital tools to represent, explore, and deepen student understanding of math concepts. <input type="checkbox"/> Help students make sound decisions concerning the use of specific tools by discussing the insight that could be gained using the tool as well as the limitations of the tool.
Seeing Structure and Generalizing	7. Look for and make use of structure	<input type="checkbox"/> Look for a pattern or structure in a mathematical object and use it to develop an efficient strategy to solve a problem. <input type="checkbox"/> Shift perspectives to see things (e.g., numbers, expressions, shapes, graphs, etc.) as a single object or compositions of several objects.	<input type="checkbox"/> Ask students to Notice & Wonder when introducing a task. <input type="checkbox"/> Provide opportunities for students to demonstrate flexibility in representing mathematics in different ways.
	8. Look for and express regularity in repeated reasoning	<input type="checkbox"/> Look at the reasoning involved in a process or sequence of steps and notice when calculations are repeated, then create shortcuts or general methods based on the repeated calculations. <input type="checkbox"/> See the overall process of solving a problem using repeated reasoning while still attending to the details. <input type="checkbox"/> Continually evaluate the reasonableness of intermediate results.	<input type="checkbox"/> Encourage students to organize and record calculations so they can more easily see when they are repeated. <input type="checkbox"/> Ask students to describe the processes they used and to look for repetition in those processes.