

L.O.: Students will take detailed constructive notes on **Exam-1: Rational Exponents, Radicals, & Complex Numbers**. Students will practice over the weekend on HMH Player (my.hrw.com) to deepen their understanding of each concept for Exam-1 that is in class on Monday.

BY: STUDY-HACK.COM

# MAKING & USING A STUDY GUIDE for a test

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Study Guide: helps you ① summarize, ② visualize, and analyze ③ concepts learned in class

\* Warning: simply making a study guide does not guarantee you an A+ on the test.

**Coursework will be weighted as follows:**

<b>1. Homework</b>	20%						
<b>2. Quizzes</b>			10%				
<b>3. Chapter Test</b>			60%				
<b>4. Final Exam</b>					10%		
<b>Total:</b>	20%	+	70%	+	10%	=	100%

Exam grade = Class grade

*Did Not Finish*  or **FAILED IT**  
 = **RETAKE IT TILL YOU MAKE IT!** @ **LUNCH TIME**

**#1.** Add the complex numbers.

$$(18 + 15i) + (-9 - 11i) = \boxed{9} + \boxed{4}i$$

Rearrange to group like terms together.

$$\begin{array}{r} 18 + 15i \\ -9 - 11i \\ \hline 9 + 4i \end{array}$$

Combine like terms.

**#2.** Add the complex numbers.

$$(-7 - 2i) + (-11 + 9i) = \boxed{-18} + \boxed{7}i$$

Rearrange to group like terms together.

$$\begin{array}{r} -7 - 2i \\ -11 + 9i \\ \hline -18 + 7i \end{array}$$

Combine like terms.



### #3. Subtract.

Distribute the "negative sign"

$$(2 + 4i) - 1(11 - i)$$
$$2 + 4i - 11 + i$$

Rearrange to group like terms together.

$$\begin{array}{r} 2 + 4i \\ -11 + i \\ \hline -9 + 5i \end{array}$$

Combine like terms.

The difference is  $-9 + 5i$ .

## #4. Subtract.

$$(-8 - 2i) - (-10 - 5i)$$

$$-8 - 2i + 10 + 5i \quad \text{Distribute the "negative sign"}$$


Rearrange to group like terms together.

$$\begin{array}{r} -8 - 2i \\ 10 + 5i \\ \hline 2 + 3i \end{array}$$

Combine like terms.

The difference is .

## #5. Subtract.

$$(6 + 6i) - (6 - 6i)$$


$$6 + 6i - 6 + 6i$$

Distribute the "negative sign"

Rearrange to group like terms together.

$$\begin{array}{r} \cancel{6} + 6i \\ -\cancel{6} + 6i \\ \hline 12i \end{array}$$

Combine like terms.

The difference is .

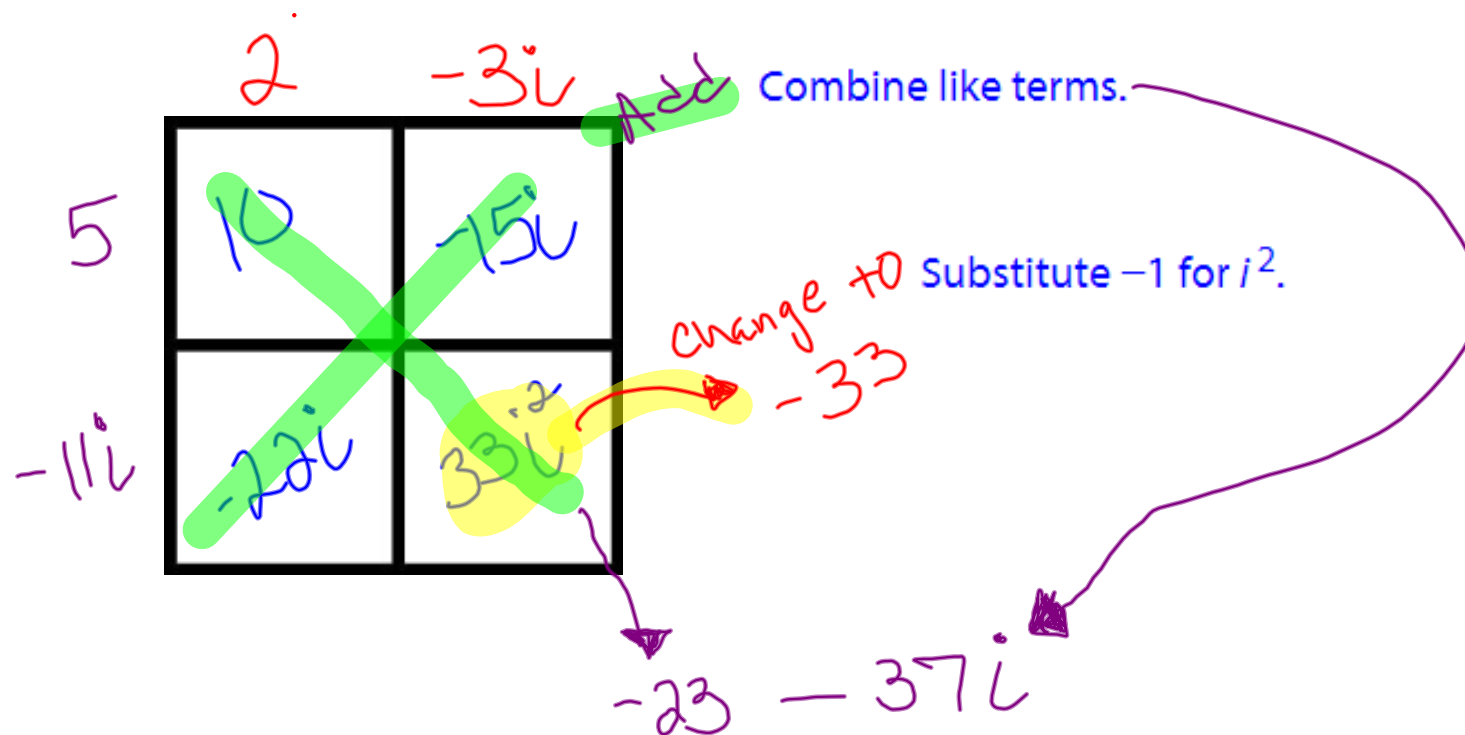


## #6. Multiply the complex numbers.

$$(2 - 3i)(5 - 11i) = \boxed{-23} - \boxed{37}i$$

$i^2 = -1$

Use the "Box method" (FOIL)



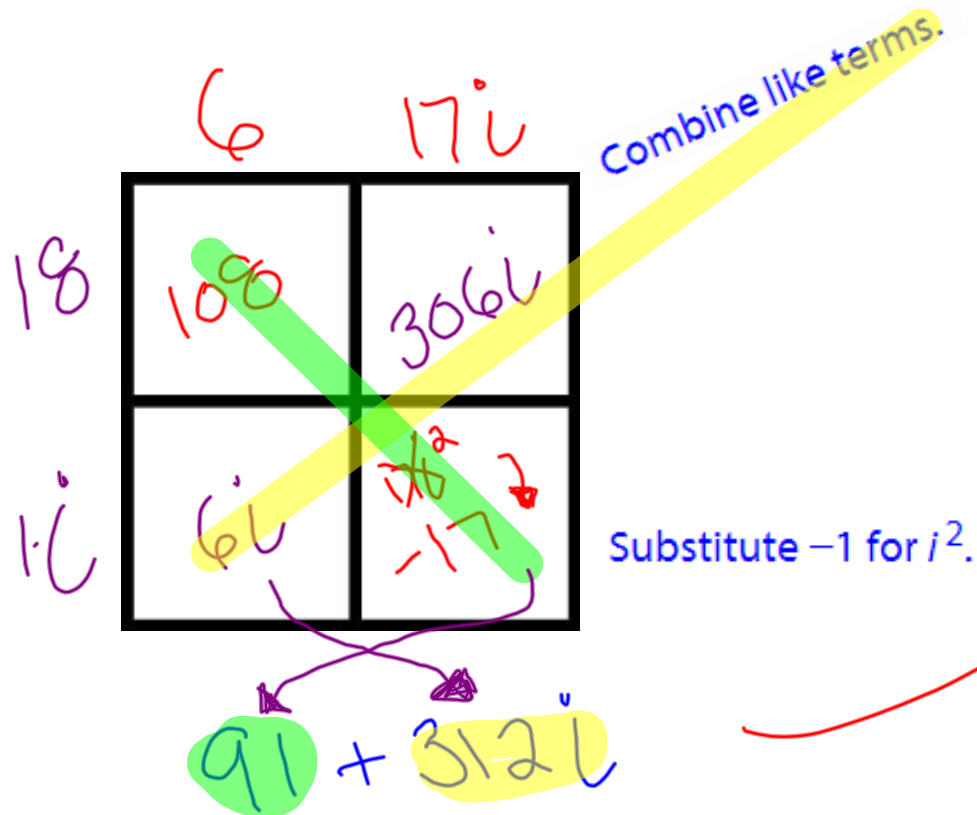
\*Multiply the edges, but add on the diagonals



**#7.** Multiply the complex numbers.

$$(6 + 17i)(18 + i) = \boxed{91} + \boxed{312}i$$

Use the "Box method" (FOIL)

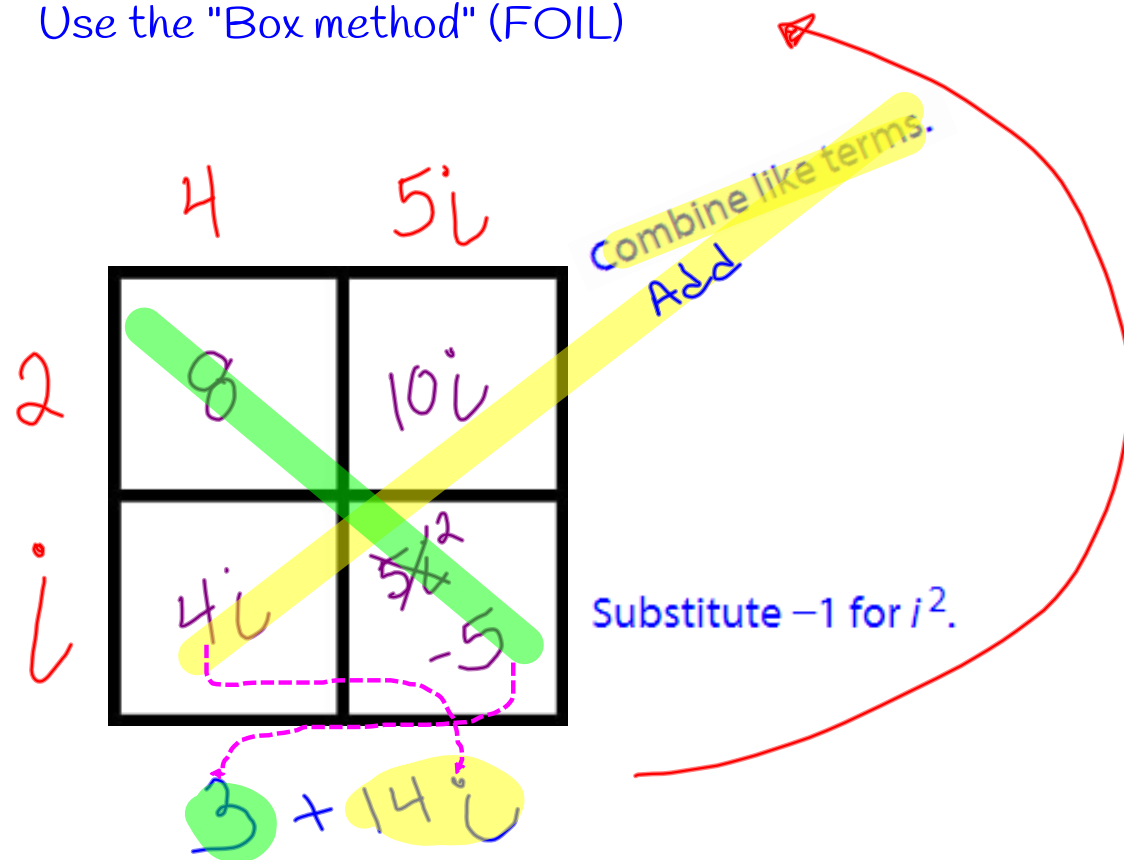


\*Multiply the edges, but add on the diagonals

#8. Multiply  $4 + 5i$  and  $2 + i$ .

$$(4 + 5i)(2 + i) = \boxed{3} + \boxed{14}i.$$

Use the "Box method" (FOIL)



\*Multiply the edges, but add on the diagonals

**#9.** Evaluate the expression for the given value of the variables.

$7a + b^2$  for  $a = -2$  and  $b = 6$ .

$7(-2) + (6)^2$

Substitute  $-2$  for  $a$  and  $6$  for  $b$

same as  
 $6 \cdot 6$

$-14 + 36$

Multiply

$22$

Add

The value of the expression is  $22$ .

#10. Find the root and simplify the expression.

$$625^{\frac{1}{4}}$$

The radical is

$$\sqrt[4]{625}$$

$$X^{\frac{a}{b}} = \sqrt[b]{X^a}; (n \neq 0)$$

Index

Exponent

Radical Symbol

Radicand

$$625^{\frac{1}{4}} = 5$$

Definition of  $n^{\text{th}}$  root.

$$\sqrt[4]{5 \cdot 5 \cdot 5 \cdot 5} = \sqrt[4]{5^4} = 5$$

\*same index and exponent cancel out each other

# #11. Simplify expressions with fractional exponents.

$$1,024^{\frac{4}{5}} = \boxed{256}$$

rewrite the base as multiplication

Rewrite radicand as a power.

Definition of  $n^{\text{th}}$  root.

The handwritten solution shows the following steps:

- Step 1:  $(\sqrt[5]{1024})^4$  with a red arrow pointing from the number 1024 to the number 4.
- Step 2:  $(\sqrt[5]{4 \cdot 4 \cdot 4 \cdot 4 \cdot 4})^4$  with a red arrow pointing from the number 4 to the number 4.
- Step 3:  $(\sqrt[5]{4^5})^4 = 4^4$  with a red arrow pointing from the number 5 to the number 4.
- Step 4:  $4 \cdot 4 \cdot 4 \cdot 4 = 256$  with the number 256 circled in yellow.

## #12. Evaluate the expression.

$$\left(\frac{1}{4}\right)^{-4} = \boxed{256}$$

Take the reciprocal "Flip" Exponent changes sign to opposite

$$(4)^4 = 4 \cdot 4 \cdot 4 \cdot 4$$
$$16 \cdot 16$$
$$256$$

**#13.** Evaluate the expression.

$$(-9)^0 = \boxed{\text{ONE!}}$$

Note

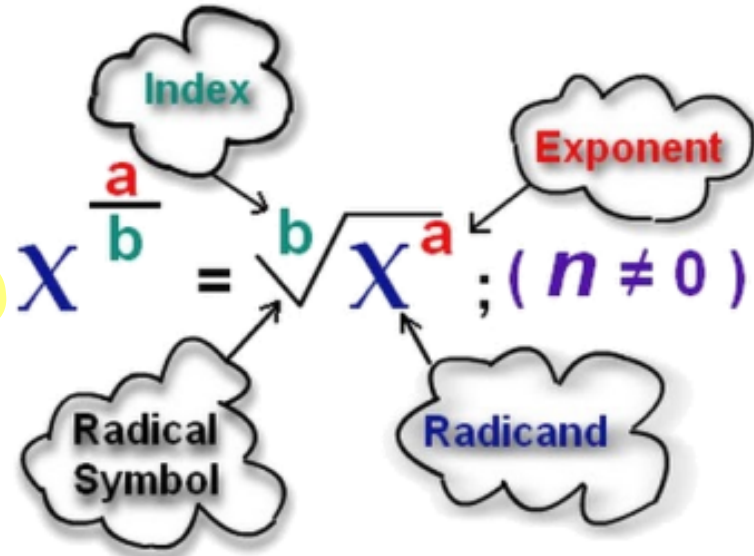
Any non-zero number raised to the power of 0 is 1.

$$x^0 = 1 \text{ for } x \neq 0.$$

**#14.** Find the root(s) and simplify the expression.

$$625^{\frac{1}{4}} + 16^{\frac{1}{2}}$$

The radical is  $\sqrt[4]{625} + \sqrt{16}$



$$625^{\frac{1}{4}} + 16^{\frac{1}{2}} = \boxed{9}$$

Handwritten work showing the simplification process:

$$\sqrt[4]{5 \cdot 5 \cdot 5 \cdot 5} + \sqrt{16}$$

$$\sqrt[4]{5^4} + \sqrt{16}$$

$$5 + 4 = 9$$

Rewrite radicands as powers.



# #15. Simplify the expression.

$$(1)^{\frac{2}{3}} = \boxed{\text{ONE}}$$

Take the reciprocal "Flip" Exponent changes sign to opposite

$$(1)^{\frac{3}{2}} = 1$$

\*Any number with base one to the power is always one, except zero.

# #16. Simplify the expression.

$$\left(\frac{1}{16}\right)^{\frac{5}{2}} = \boxed{1024}$$

Take the Reciprocal (Flip)

Same thing

$$\sqrt[2]{a} = \sqrt{a}$$

$$(16)^{\frac{5}{2}}$$

Convert to radical.

$$\left(\sqrt[2]{16}\right)^5 = (4)^5 = 4 \cdot 4 \cdot 4 \cdot 4 \cdot 4$$
$$= 16 \cdot 16 \cdot 4$$
$$= 256 \cdot 4 = 1024$$

Same as Square Root

**#17.** Simplify each expression. Assume all variables are positive.

Distribute the power

$$(x^5 y)^5 \sqrt{y^6} = x^{\boxed{25}} y^{\boxed{6}}$$

$$x^{5 \cdot 5} \quad y^{1 \cdot 5} \quad \downarrow \quad y$$

$$x^{25} \cdot y^5 \cdot y^1$$

like base

$$x^m \cdot x^n = x^{m+n}$$

$$x^{25} \cdot y^6$$

**#18.** Simplify each expression. Assume all variables are positive.

$$\frac{\sqrt[2]{x^6}}{\sqrt[2]{x^4}} = x^{\boxed{1}}$$

$$\frac{x^{\frac{6}{2} \text{ reduce}}}{x^{\frac{4}{2} \text{ reduce}}}$$

Rewrite using rational exponents.

$$\frac{x^3}{x^2}$$

$$= x^{3-2} = x^1$$

When you divide by the same base, subtract the exponents:

$$\frac{a^m}{a^n} = a^{m-n}$$

**#19.** Simplify the expression. Assume all variables are positive.

$$\left( \frac{1}{4x^4} \cdot x^{20} \right)^{-\frac{1}{2}} = \boxed{\phantom{00}} \frac{2}{x^8} \boxed{\phantom{00}}$$

Cross cancel the x's

$$\left( \frac{x^{16}}{4} \right)^{-\frac{1}{2}}$$

Take the Reciprocal (Flip)

$$\left( \frac{4}{x^{16}} \right)^{\frac{1}{2}}$$

Exponent changes sign to opposite

Square Rt  
TOP/BOTTOM =  $\frac{2}{x^8}$

## #20. Simplify the given expression.

Distribute the power, cancel the x's...

$$\left( (3x)^1 (3x)^2 \right) = \boxed{27} x \boxed{3}$$

$$(3x)^1 \cdot (3x)^2 = (3x)^3 = 3^3 x^3 = 27x^3$$

*(Note: 3·3·3 is written below the 3<sup>3</sup> term)*

$$a^m \cdot a^n = a^{m+n}$$

**#21.** Simplify the expression.

$$216^{\frac{1}{3}} - 125^{\frac{1}{3}} = \boxed{1}$$

Convert to radicals.

$$\sqrt[3]{216} - \sqrt[3]{125}$$

Rewrite radicands as powers.

$$\sqrt[3]{6^3} - \sqrt[3]{5^3}$$
$$6 - 5 = 1$$

## #22.

A baker sells bread for \$5 a loaf and rolls for \$1 each. The baker needs to sell \$55 worth of baked goods by the end of the day.

Enter a linear equation that describes the problem.

An equation for the value of the baked goods is   = \$55, where  $b$  is the number of loaves of bread sold, and  $r$  is the number of rolls sold.

$5b + r$

Notes  
Do not put one in front of  $r$ .

$5b + 1 \cdot r$



## #23.

A movie theater sells tickets to a new show for \$12 each. The theater also sells small containers of popcorn for \$5 each. The theater needs to make \$3167 in order to break even on the show.

Enter a linear equation that describes the problem.

An equation for the amount of money earned by the movie theater is

= \$3167, where  $t$  is the number of tickets sold, and  $p$  is the number of popcorn buckets sold.

$\$12t + \$5p$

#24. Simplify  $7vw^3 \cdot 3v^4$ .

$$7v^1w^3 \cdot 3v^4 = \boxed{\phantom{0000}}$$

$$7 \cdot 3 \cdot v^5 \cdot w^7$$

$$= 21v^5w^7$$

Add exponents when multiplying.

#25. Find the slope and y-intercept.

$$y - 6 = 2x + 4$$

$+6$                        $+6$

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$$y = 2x + 10$$

$$\text{Slope} = 2$$

$$y\text{-int} = 10$$

moving the constants to one side.

$$y = mx + b$$

↑                      ↑  
slope                  y-  
intercept

$$m = \frac{y_2 - y_1}{x_2 - x_1} \quad (0, b)$$

AAA